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# On Implementing Open World Semantic Differencing for Class Diagrams

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## ABSTRACT

Semantic difference analyses support engineers in understanding model-changes on the semantic level and thereby assist change management in Model Driven Development (MDD). A semantic differencing operator for Class Diagrams (CDs) compares two input models based on their legal instances and outputs object structures that are permitted by the first but not the second input-CD. Under the closed-world assumption only instances of explicitly-modeled elements are permitted. This closed-world approach may be less suited for semantic refinement checking in early design phases, where new elements are added to a CD in order to refine it. Instead, an open-world approach can be utilized. In this paper, we outline, evaluate and compare two approaches for extending CDDiff, an existing closed-world semantic differencing operator for CDs, to an open-world operator: The first approach reduces the open-world problem to a bounded search via Alloy. The second approach transforms the input-CDs and reduces the open-world problem to closed-world semantic differencing. It also allows for combining open- and closed-world interpretations of model-elements.

KEYWORDS class diagrams, uml, difference analysis, semantics, model-driven development, cddiff.

## 1. Introduction

Models are the primary artifacts of MDD. As such, they evolve over the course of the development process. To assist in effective change management, differencing operators can be utilized. While syntactic differencing operators are useful and commonplace (Alanen & Porres 2003; Kehrer et al. 2011; T. Kehrer, U. Kelter, and G. Taentzer 2013; Küster et al. 2009, 2008; Taentzer et al. 2014; Thüm et al. 2009), they do not necessarily reveal the semantic difference of two models, *i.e.*, the difference in their 'meaning' (Harel & Rumpe 2004). To better understand model-changes on a semantic level, one may employ semantic differencing operators.

Maoz et al. (2011b) introduced CDDiff, a semantic differencing operator for UML/P CDs (Rumpe 2011). This operator is based on a formal semantics definition for UML/P CDs that maps each model to a set of legal instances, *i.e.*, the set of object structures the CD permits. The (asymmetric) semantic difference of two CDs is then given as the set of object structures permitted by the first and not the second CD. The object structures in this set are also referred to as diff-witnesses. If no diff-witness exists, *i.e.*, if the semantics of the first CD is contained in the semantics of the second CD, we say that the first CD (semantically) refines the second CD (Herrmann et al. 2007; Kautz & Rumpe 2018a). The implementation of CDDiff relies on a translation to Alloy (Jackson, Daniel 2006; Kautz et al. 2017) in order to find diff-witnesses. These witnesses are presented as textual UML/P Object Diagrams (ODs).

CDDiff originally only operated under the closed-world assumption, *i.e.*, object structures were not permitted to instantiate types, attributes and associations not explicitly modeled in the corresponding CD (Reiter 1978). As discussed by Nachmann et al. (2022), this becomes less suitable in early design phases of the development process. Here, new elements are often added to models in order to refine them. This notion of refinement,

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however, does not correspond to semantic refinement under the closed-world assumption. Instead, an open-world approach is needed that considers each CD as underspecified. This way, objects structures are permitted to instantiate types as well as association not modeled in the CD. Thus, the addition of new elements to the CD constitutes a semantic refinement.

The open-world assumption complicates the implementation of a semantic differencing operator, as the semantics of a CD now includes instances of infinitely many types and associations. Fahrenberg et al. (2014) circumvent this problem by computing a difference-CD that includes only those syntactic elements that may induce a semantic difference. This, however, does not allow for producing concrete diff-witnesses in the semantic domain of the analyzed CDs.

In order to realize a semantic differencing operator for CDs that can compute diff-witness under the open-world assumption, we reduce the problem of open-world semantic differencing by restricting diff-witnesses in size and scope, as typical to bounded analyses such as the original implementation of CDDiff (Maoz et al. 2011b).

Our contributions include two approaches for extending CDDiff to an open-world semantic differencing operator for finitely satisfiable CDs (Balaban & Maraee 2013) and are listed as follows:

- 1. For our first approach, we extend CDDiff's translation of CDs to Alloy to allow for open-world semantic differencing. Instead of fully specifying the CDs in Alloy, our new translation encodes underspecification and thus it also considers possible CD-expansions (Nachmann et al. 2022).
- 2. For our second approach, we reduce the problem of openworld semantic differencing to its closed-world variant by transforming the input-models.
- 3. We extend the transformation to allow for combining closed-world and open-world interpretation of model-elements via stereotypes.

The implementation of the extended CDDiff-operator is part of the CD4Analysis-project which is publicly available at: https://github.com/MontiCore/cd4analysis

The remainder of the paper is structured as follows: In Sect. 2, we discuss related work concerning semantic differencing. Next, in Sect. 3, we present a motivating example for open-world semantic differencing in the context of designing a reference model for digital twins. The abstract syntax and formal semantics for the notion of CDs used in this paper is defined in Sect. 4. In Sect. 5 we outline changes made to the translation of CDs to Alloy in order to include additional type-information for objects. We introduce our first approach for open-world semantic differencing in Sect. 6. In Sect. 7 we present our second approach: a reduction of the open-world problem of semantic differencing of CDs to closed-world semantic differencing. We evaluate and compare the diff-witnesses and performance of both approaches in Sect. 8 and, finally give a conclusion and outlook in Sect. 9.

## 2. Related Work

Harel & Rumpe (2004) characterize the relationship between

syntax and semantics of modeling languages as a semantic mapping that maps each syntactically valid model to a subset of a well-defined and well-understood semantic domain. For CDs we consider a semantic domain consisting of object structures that correspond to possible data-states of a software system.

Maoz et al. (2011b) introduce CDDiff, a semantic differencing operator for UML/P CDs that can detect semantic differences of two CDs under a closed-world assumption. It produces diff-witnesses in the form of UML/P ODs describing object structures permitted by the first CD that are not permitted by the second CD. The operator utilizes a translation to Alloy in order to find these object structures using the Alloy Analyzer. The translation rules are outlined in (Kautz et al. 2017).

Nachmann et al. (2022) suggest that open-world semantic differencing might be well-suited for refinement-checking in early design phases, were new elements might be added to the sourcemodels precisely in order to refine them. An expansion-based semantics is proposed to more accurately reflect underspecification of CDs and to prevent inconsistent type-inheritance within object structures.

Fahrenberg et al. (2014) present a merge and differencing operator for CDs. Open-world semantic refinement of the component-CDs is considered as a soundness-condition for the merge. The notion of syntactic refinement is used as a sufficient condition for semantic refinement. This notion is similar to that of CD-expansion (Nachmann et al. 2022). Unlike CDDiff (Maoz et al. 2011b), the differencing operator presented here does not produce witnesses in the semantic domain. Instead, it outputs a diff-CD that contains only syntactic elements of the first input-CD that induce a semantic difference when compared to the second input-CD. Moreover, the semantic implications of association directions are not considered.

Drave, Kautz, et al. (2019) outline both a closed-world and an open-world semantic differencing operator for Feature Models (FMs). The latter is realized by reducing the problem of open-world semantic differencing to a finite subset.

ADDiff, a semantic differencing operator for Activity Diagrams (ADs), was introduced in (Maoz et al. 2011a). It uses a translation to SMV, outlined in (Maoz et al. 2011c), and computes execution traces that constitute diff-witnesses. The paper presents two algorithms for computing these diff-witnesses: a concrete forward-search algorithm and a symbolic fixed-point algorithm. Kautz & Rumpe (2018b) present an alternative approach to ADDiff that considers a smaller subset of ADs and reduces the problem of semantic differencing to language inclusion checking and counterexample generation for finite automata. Both approaches operate under a closed-world assumption. Language inclusion checking and counterexample checking for finite automata is also used in (Drave, Eikermann, et al. 2019) to realize semantic differencing for UML/P State-Charts (SCs) with finite input- and output-alphabets as well as in (Kautz 2021) for Sequence Diagrams (SDs). Using a translation to Büchi automata instead, the same can be achieved for Time-Synchronous Port-Automata (TSPA) with finite input-/output-alphabets and state-space (Butting et al. 2017).

Langer et al. (2014) present a generic approach for semantic differencing that utilizes existing semantics specification approaches in order to define the behavioural semantics of a particular modeling language. The models are then executed and compared regarding their execution traces. If additional input is required for concrete execution, the authors propose using symbolic execution to automatically generate relevant inputs. Their approach is demonstrated using the semantics specification language xMOF to realize a semantic differencing operator for Petri nets. Moreover, with this generic approach differencing operators for CDs and ADs were implemented according to the specifications of ADDiff and CDDiff, as well. Their performance was, however, ultimately weaker than the original approaches in (Maoz et al. 2011b,a)

We observe relations between open-world CD semantics and various meta-model extensions. Jiang et al. (2004) define four levels of meta-model extensions. Bruneliere et al. (2015) present operators for meta-model extension and two approaches for managing instances of modified meta-models. Jácome-Guerrero & de Lara (2018) introduce rules to control meta-model extensibility. The four levels from (Jiang et al. 2004) rely on extensions of meta-models that are also allowed by open-world semantics of CDs. Most additive operations from (Bruneliere et al. 2015) and four out of the eight meta-model customization from (Jácome-Guerrero & de Lara 2018) are supported by our open-world semantics. However, Bruneliere et al. (2015) and Jácome-Guerrero & de Lara (2018) support deletions of elements, which are not captured in the open-world differencing semantics. It might be interesting future work to investigate semantic differencing of CDs with case-specific customization operations of meta-models instead of generic rules for open-world semantics.

Finally, another line of work investigates model typing (Steel & Jézéquel 2007) and subtyping (Guy et al. 2012) relations. In contrast to most meta-model extensions, these works focus on a type-like compatibility on the instance level. Comparing instances of models with compatible types (Steel & Jézéquel 2007) might be supported by CDDiff following similar adjustments as we did for open-world semantics, while model subtyping of (Guy et al. 2012) supports type adaptation, which is likely difficult to discover automatically.

## 3. Motivating Example

We motivate the use of open-world semantic differencing for CDs with an example: A team of engineers aims to design a CD capturing a reference model for digital twins. Among others, the engineers must represent the following requirements:

- 1. A digital twin has exactly 1 machine as its original.
- A digital twin consists of a set of digital shadows and models.

The engineers construct CD v1 shown in Figure 1 consisting of the classes DigitalTwin, Machine, DigitalShadow and Model with appropriate relations.

The following additional requirements are discovered:

- 1. A digital twin consists of at least 1 model and digital shadow.
- 2. A digital shadow consists of a non-empty set of data traces.

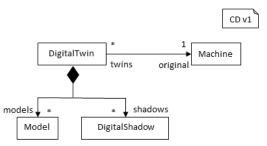


Figure 1 Initial reference-CD for a digital twins.

- 3. A data trace corresponds to exactly 1 machine.
- 4. A model is either a data model or a process model.

As a consequence, the engineers add the classes DataModel, ProcessModel and DataTrace as well as corresponding relations to the original CD v1. Class Model is changed into an abstract class resulting in CD v2 shown in Figure 2.

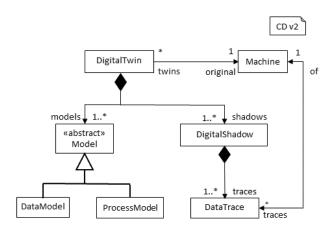
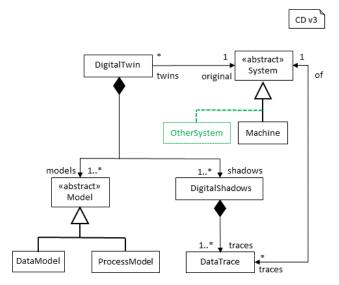


Figure 2 Subsequent reference-CD for digital twins.

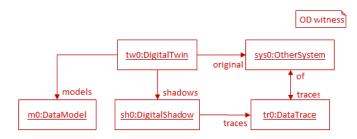
The team analyzes the semantic difference between CD v1and CD v2 and learns that with closed-world semantics the CDs are incomparable as each allows instances not allowed by the other. However, the closed-world assumption might not be appropriate here as one might expect that CD v1 is incomplete and that further classes and relations may be added. With the open-world assumption CD v2 depicted in Figure 2 is a refinement of CD v1 depicted in Figure 1. As an example, objects of class DataModel are not permitted in the closedworld semantics of v1, as the class is not part of the CD. They are, however, included in both the closed-world and open-world semantics of CD v2.

After some reconsideration, the team decides that machines are not the only type of system to have a digital twin. They attempt to refactor the CD by inserting the abstract class System that is then extended by the class Machine. The association that previously targeted Machine is now pulled up in the inheritance hierarchy to class System in CD v3 shown in Figure 3.

This change indeed is a refactoring according to closedworld semantics (Maoz et al. 2011b; Nachmann et al. 2022), i.e.,  $cddiff(v2, v3) = cddiff(v3, v2) = \emptyset$ . However, un-



**Figure 3** Attempted refactoring of the reference-CD for digital twins.



**Figure 4** Object structure in the open-world semantics of the CD v3 (Figure 3) that constitutes a diff-witness for the semantic difference between the CD v2 (Figure 2) and CD v3.

der an open-world assumption, a DigitalTwin is permitted to have an original in CD v3 that is not a Machine, i.e.,  $cddiff(v2, v3) \neq \emptyset$ , as demonstrated by the diff-witness, an object structure, shown in Figure 4.

This contradicts the first requirement, which states that a digital twin has exactly 1 machine as its original. Consequently, the object structure in Figure 4 is not permitted by CD v1 nor by CD v2, which accurately reflect the requirement. Thus, the change does neither constitute a refinement in the closed world nor in the open world. The object structure serves as a witness for the semantic difference between the versions CD v2 and CD v3 of the reference model depicted in Figure 2 and Figure 3, respectively. The team has to either reverse the design step or revise their initial requirements.

## 4. Syntax and Semantics of Class Diagrams

The following definitions closely follow the definitions provided by (Nachmann et al. 2022) and (Maoz et al. 2011b). However, some changes to the abstract syntax and semantics were introduced, *e.g.*, we extended the abstract syntax and semantics from (Nachmann et al. 2022) to support anonymous, directed associations and refined the semantic domain. Each subsection discusses the changes compared to (Nachmann et al. 2022) motivated by new features that were added or features of the differencing operator from (Maoz et al. 2011b).

#### 4.1. Abstract Syntax of Class Diagram

CDs are widely used to model the structure of object-oriented software systems. They define the set of all possible object structures that comprise a potential data state of a system (Rumpe 2011). In this section we review the abstract syntax of CDs based on the UML/P variant defined in (Rumpe 2011).

A CD defines a finite set of classes, as well as a finite set of associations between those classes. A class may extend other classes, thus inheriting all associations of its super-classes. Moreover, classes may be declared abstract such that they cannot be instantiated directly. We consider unidirectional and bidirectional binary associations. A binary association references two classes and has a role name and a cardinality for each side. The cardinality imposes constraints on the number of allowed instances (*i.e.*, links) from the same object.

Extending (Nachmann et al. 2022), we also consider anonymous as well as directed associations. As such, let C be a universe of class names and N a universe of role names. Moreover, let  $\mathcal{I}$  be the set of all finite unions of finite or unbounded intervals of natural numbers. We formally denote the abstract syntax of CDs as follows:

**Definition 4.1** (Abstract Syntax of Class Diagrams). *Given a Class Diagram cd we declare that* 

- 1. cd.classes  $\subseteq C$ : denotes the finite set of class declarations in cd,
- cd.abstract ⊆ cd.classes: denotes the subset of classes declared abstract in cd,
- *3.* cd.assoc ⊆ cd.classes × N × N × cd.classes: denotes the finite set of directed associations in cd,
- 4. cd.bidir ⊆ cd.assoc: denotes the finite subset of bidirectional associations with (c<sub>1</sub>, r<sub>1</sub>, r<sub>2</sub>, c<sub>2</sub>) ∈ cd.bidir ⇔ (c<sub>2</sub>, r<sub>2</sub>, r<sub>1</sub>, c<sub>1</sub>) ∈ cd.bidir,
- cd.cardL : cd.assoc → I and cd.cardR : cd.assoc → I define the cardinality for the left side and the right side of an association respectively,
- 6.  $c_1 \prec_{cd} c_2$ : denotes that a class  $c_1$  directly extends another class  $c_2$  in cd.

The reflexive transitive hull of the extends-relation  $\prec_{cd}$  is denoted by  $\prec^*_{cd}$  and must define a partial ordering on cd.classes.

Consider for example the CD v3 depicted in Figure 3, the set of class declarations is then denoted as v3.classes and contains the classes DigitalTwin and System. The class System is declared abstract and thus also included in v3.abstract. The unidirectional association connecting DigitalTwin and System is denoted by the tuple a := (DigitalTwin, twins, original, System) with  $v3.cardL(a) = [0, \infty)$  and v3.cardR(a) = [1, 1]. The bidirectional association between classes System and DataTrace is denoted by tuples (System, of, traces, DataTrace) and (DataTrace, traces, of, System), which are contained in

v3.bidir. The class Machine directly extends the abstract class System which is denoted by Machine  $\prec_{v3}$  System.

We have omitted elements of UML/P CDs from this definition to fit the scope of this paper. In the following, we list these model-elements and justify their exclusion. Note that the majority of these elements are supported by our implementation.

- Attributes and composition are handled analogous to associations.
- Interfaces are handled analogous to abstract classes.
- CDDiff considers enumerations as sets of values. Under the open-world assumption new enumerations can be added to the CD, and existing enumerations can be expanded by introducing arbitrary new constants. Thus, they do affect the open-world semantics of a CD.
- Underspecified cardinalities were not included in the abstract syntax as they are semantically equivalent to  $[0, \infty)$ when considering valid instances of the CD.
- Additionally, we do not consider underspecification of association direction and role names. These are given a default specification by our implementation.
- Finally, CDDiff does not consider method-signatures as they are not part of the data-structure instances. As such, they are not included here, either.

#### 4.2. Semantics of Class Diagrams

We consider a semantics for CDs that maps each model to a set of legal instances, *i.e.*, the set of objects structures that it permits (Harel & Rumpe 2004; Maoz et al. 2011b; Nachmann et al. 2022). Moreover, we distinguish between the closed-world semantics, which only permits instances of explicitly modeled elements, and open-world semantics, which considers CDs to be underspecified and thus permits instances of other, undeclared types and associations, as well.

**4.2.1. Semantic Domain** Object structures represent potential data states of an object-oriented system and thus form the semantic domain for CDs. An object structure consists of a finite set of objects, as well as a finite set of directed links. Each object instantiates a set of classes and has a most-specific type. Formally, we denote object structures as follows:

**Definition 4.2** (Abstract Syntax of Object Structures). *An object structure os consists of* 

- *1. a finite set of objects os.obj such that for each*  $o \in os.obj$ 
  - (i)  $o.types \subseteq C$  denotes the set of all types that o instantiates,
  - (ii) and o.type  $\in$  o.types denotes its most-specific type,
- 2. as well as a finite set of links between objects: os.links  $\subseteq$  os.obj  $\times \mathcal{N} \times$  os.obj.

Consider for example the object structure witness modelled by the OD in Figure 4 with witness.obj =  $\{tw0, sys0, m0, sh0, tr0\}$ . The most-specific type of the object m0 is m0.type = DataModel and since witness is an instance of the CD v3 depicted in Figure 3, we can infer that Model  $\in$  m0.types. The object m0 is also target of a link from tw0, i.e., (m0, models, tw0)  $\in$  witness.links.

#### 4.3. Closed-World Semantics

An object structure is a legal instance of a CD according to its closed-world semantics iff the following conditions hold: Each object within the object structure only instantiates classes of the CD, (2) the most specific type of each object corresponds to a non-abstract class, (3) each link corresponds to an association and (4) the cardinality constraints of each association are respected. More formally:

**Definition 4.3** (Closed-World Semantics of Class Diagrams). An object structure os is a closed-world instance of a Class Diagram cd iff os satisfies the following constraints:

- For every object o ∈ os.obj, it holds that
   (i) o.type ∈ cd.classes\cd.abstract,
   (ii) o.types ⊆ cd.classes.
- 2. For every object  $o \in os.obj$ , it holds that  $t \in o.types \iff o.type \prec_{cd}^* t$ .
- 3. For every link  $(o_1, r_2, o_2) \in os.links$ , there is an association  $a \in cd.assoc$  with  $a = (c_1, r_1, r_2, c_2)$  such that  $c_1 \in o_1.types$  and  $c_2 \in o_2.types$ .
- 4. For each association  $a := (c_1, r_1, r_2, c_2) \in cd.assoc$ and each  $o_2 \in os.obj$  with  $c_2 \in o_2.types$ , it holds that  $|\{(o_1, r_2, o_2) \in os.links : c_1 \in o_1.type\}| \in cd.cardL$
- 5. For each association  $a := (c_1, r_1, r_2, c_2) \in cd^{\rightarrow}$ .assoc and each  $o_1 \in os.obj$  with  $o_1$ .type  $\prec_{cd}^* c_1$ , it holds that:
  - (i)  $(o_1, r_2, o_2) \in os.links \implies c_2 \in o_2.types$
  - (*ii*)  $|\{(o_1, r_2, o_2) \in os.links\}| \in cd.cardR$
- 6. For  $a = (c_1, r_1, r_2, c_2) \in cd.bidir and o_1, o_2 \in os.obj$ with  $c_1 \in o_1.type$  and  $c_2 \in o_2.types$ , we have:  $(o_1, r_2, o_2) \in os.links \iff (o_2, r_1, o_1) \in os.links.$

The closed-world semantics  $[cd]^{cw}$  of cd is the set of all closed-world instances.

Consider again our motivating example from Sect. 3, unless OtherSystem is included in v3 (Figure 3), the object-structure witness (Figure 4) would not constitute a closed-world instance, since sys0.type  $\notin v3.classes$ .

With the previous definition of CD semantics, we may now characterize a closed-world refinement of a CD as follows:

**Definition 4.4** (Closed-World Refinement). We say that a Class Diagram A is a refinement of a Class Diagram B under the closed-world assumption iff  $[A]^{cw} \subseteq [B]^{cw}$ .

We assume that the open-world operator's input-CDs are finitely-satisfiable under a closed-world assumption, *i.e.*, that each class of an input-CD can be instantiated according to the closed-world semantics (Balaban & Maraee 2013). We use this assumption for proving the completeness of the reduction from open-world semantic differencing to closed-world semantic differencing in Sect. 7. This ensure the existence of diff-witnesses in the open world iff they are present for the reduced problem instance in the closed world.

**Definition 4.5** (Finite Satisfiability (Balaban & Maraee 2013)). A class  $c \in C$  is finitely-satisfiable in a CD cd iff there exists an object structure  $os \in [[cd]]^{cw}$  with an object  $o \in os.obj$  such that  $c \in o.types$ . CD cd is finitely-satisfiable iff every class  $c \in cd.classes$  is finitely-satisfiable.

## 4.4. Open-World Semantics

We consider an expansion-based open-world semantics for CDs (Nachmann et al. 2022). This not only ensures consistency of type-inheritance within object structures, but also more accurately reflects the notion of underspecification.

**Definition 4.6** (Open-World Semantics of Class Diagrams). An object structure os is an open-world instance of a Class Diagram cd iff there exists an expansion  $cd^x$  of cd (see Def. 4.8) with  $os \in [cd^x]^{cw}$ . The open-world semantics of cd, denoted as  $[cd]^{ow}$ , is the set of all open-world instances.

The notion of open-world refinement is then defined analogous to its closed-world counterpart:

**Definition 4.7** (Open-World Refinement). We say that a Class Diagram A is a refinement of a Class Diagram B under the open-world assumption iff  $[\![A]\!]^{ow} \subseteq [\![B]\!]^{ow}$ 

Intuitively, a CD-expansion preserves all existing classes, associations and extends relations, but it permits additions.

**Definition 4.8** (Expansion). A Class Diagram  $cd^x$  is an expansion of a Class Diagram cd iff

- *1.*  $cd.classes \subseteq cd^{x}.classes$ ,
- 2.  $cd.abstract \subseteq cd^x.abstract$ ,
- 3.  $cd.assoc \subseteq cd^x.assoc$
- 4. cd.bidir  $\subseteq$  cd<sup>x</sup>.bidir
- 5.  $\forall c_1, c_2 \in cd.classes : c_1 \prec_{cd} c_2 \implies c_1 \prec_{cd^x} c_2$ ,
- 6.  $\forall a \in cd.assoc : cd.cardL(a) = cd^x.cardL(a) \land cd.cardR(a) = cd^x.cardR(a)$

Referring back to our motivating example in Sect. 3, adding OtherSystem as a subclass to System in CD v3 constitutes an expansion of CD v3. The object structure *witness* from Figure 4 is an instance of this expansion in the closed world according to Def. 4.3, and thus it is an open-world instance of v3. On the other hand, when considering CD, v2, the link (tw0, original, sys0) violates the semantics of the association (Digital, twins, original, Machine) as Machine  $\notin$  sys0.*types* (see Def. 4.3). This might not be immediately clear when looking at Figure 4, as super-types are usually not depicted in ODs. To avoid ambiguity, our implementation uses the stereotype *«instanceof = ...»* in diff-witnesses produced by the open-world operator to list all types an object instantiates.

## 4.5. Overlapping Associations

Overlapping associations are permitted by the abstract syntax we defined in Sect. 4.1. Concerning our previous semantics definitions, we distinguish between refining/super-associations and conflicting association.

**Definition 4.9** (Refining and Super-Association). An association  $a' = (c'_1, r'_1, r_2, c'_2)$  refines another association a :=

 $(c_1, r_1, r_2, c_2)$  with respect to a class diagram cd iff (1)  $c_1 \prec_{cd}^* c'_1, c_2 \prec_{cd}^* c'_2$  and (2)  $a, a' \in cd.bidir \implies r_1 = r'_1$ . In this case, we also refer to a' as a refining association and to a as a super association of a.

Refining association are a valid concept with regards to settheory: an association restricts the set of objects that can be accessed via the role name, a refining association further restricts this set for a subclass. However, for implementation purposes, this type of overriding is unfortunately not supported by most object-oriented programming languages (*e.g.*, Java).

Note special cases of *redundant* super-associations whose constraints are implied by their refining associations and *con-flicting* associations as defined in Def. 4.10.

**Definition 4.10** (Conflicting Associations). An association  $a = (c_1, r_1, r_2, c_2)$  conflicts with another association  $a' = (c'_1, r'_1, r_2, c'_2)$  with respect to a class diagram cd iff  $c_1 \prec^*_{cd} c'_1$  and either (1)  $c_2 \not\prec^*_{cd} c'_2$  or (2)  $a, a' \in cd.$  bidir and  $r_1 \neq r'_1$ . We say that a class diagram cd is conflict-free, if it contains no conflicting associations.

Unlike refining associations, conflicting associations cannot be instantiated as they induce contradicting constraints on the formal semantics of a CD.

## 5. Alloy-Based Semantic Differencing

Alloy is a textual modeling language based on relational firstorder logic (Jackson, Daniel 2006). Models are defined in Alloy modules and consist of signature declarations, fields, predicates, and facts. The Alloy Analyzer can be used to find instances of signatures that satisfy predicates and facts within a specified search-space.

CDDiff translates two CDs into an Alloy module in order to find diff-witnesses using the Alloy Analyzer (Maoz et al. 2011b; Kautz et al. 2017). The semantics of each CD are expressed by a predicate in the Alloy module. When computing a diff-witness the predicate of the first CD has to hold, while the predicate of the second CD must not. In the translation of (Kautz et al. 2017), an abstract signature 0bj is used to represent objects in the semantic domain of a CD. Each class in the input-CDs is translated into a signature that extends 0bj. Role names and attribute names in the input-CDs are translated to signatures extending an abstract signature FName (field name). The signature 0bj contains the function get that given a field name, returns a set of objects, values and enumeration-values. Predicates restrict the get-function such that it accurately encodes the semantics of associations and attributes.

Note that for executing CDDiff, a diff-size has to be specified that limits the number of instances for each top-level signature (*e.g.*, Obj). If not specified by the user, a heuristic based on the number of classes and associations in the input-CDs is used.

In order to accommodate open-world semantic differencing, we add an abstract signature Type, as shown in Listing 1, that allows us to specify and track the types instantiated by an object. The Type signature is extended by a singleton signature for each class in the input-CDs. Furthermore, an additional predicate is generated that allows specifying the reflexive transitive hull of the extends relation via the super-attribute for each input-CD, respectively. For the translation to ODs, we utilize the stereotype (instanceo f = "...") to depict all types of an object.

For example, the class DataModel in the CD v3 (Figure 3) would be translated into a sub-signature of Obj. A corresponding lone sub-signature of Type, with the name Type\_DataModel, would also be generated, containing both itself and Type\_Model in field Type\_DataModel.super. A full example-module cwdiff\_DT3\_DT2\_module.als is included in the doc-folder of the GitHub-project.

```
// object signature now includes a type-attribute
  abstract sig Obj {
    get : FName -> {Obj + Val + EnumVal},
    type: Type }
  // introduce new abstract sig Type
6
  abstract sig Type {
7
    super: set Type,
    inst : set Obj}
10
  // define the super-types for a set of objects
11
  pred ObjTypes[obj: set Obj, types: set Type]{
12
13
    all o:obj| o.type.super = types}
14
15
  // specify the instances of a type
  fact InstancesOfTypes {
16
17
    all t: Type |
      t.inst = {o:Obj | t in o.type.super}
18
19
  }
```

**Listing 1** Modifications to the generic part of the Alloy Module to enable multi-instance CD-semantics.

The complete, modified translation from CDs to Alloy with signature Type (e.g., for closed-world semantic differencing) is is implemented in class CD2AlloyGenerator<sup>1</sup>.

## 6. Solution I: Open-World Semantic Differencing with Alloy

In order to realize open-world semantic differencing in Alloy, we reduce the problem to a more restrictive, finite version of itself. This is possible since elements that are absent from both input-CDs cannot by themselves induce a semantic difference, hence we need, for the most part, only consider elements that are modelled in either CD. As such, we only use existing class and role names and permit Alloy to add new elements to the set of associations and the extends-relation. To ensure completeness, we add a new non-abstract subclass to each abstract class in the CD as well as an additional dummy class to each input-CD beforehand. This allows the Alloy Analyzer to consider all relevant expansions of the input-CDs and thus detect any semantic differences in the open world.

Note that the added non-abstract sub-classes allow indirect instantiation of abstract classes without additional constraints. Moreover, the added dummy class represents an arbitrary new class previously not present in either input-CD and is needed for certain edge cases, e.g., consider the situation in Figure 5

where adding the class Dummy to CD P1 and reusing the rolename knows from P2 allows the operator to detect the semantic difference from P1 to P2 exemplified by the OD PDiff. In PDiff, we find that Person bob knows d0, which is invalid according to P2, as b0 is not an instance of Person.

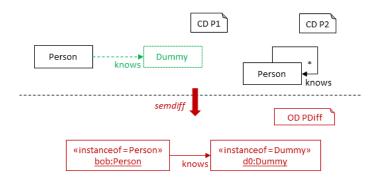


Figure 5 Example for semantic difference induced by existing association and the added dummy-class.

The correctness and soundness for this approach follow directly from the correctness and soundness of the reduction-based approach introduced in Sect. 7.

In order to implement the Alloy-based approach, we extend the class CD2AlloyGenerator via the subclass OpenWorldGenerator<sup>1</sup> and override some of the existing translation-procedures. First and foremost, we no longer restrict the get-function to associations (and attributes) defined in the respective CD, nor do we restrict objects to instances of classes in the first input-CDs. The inheritance-relation is also left underspecified. Instead, we now need to ensure anti-symmetry, reflexivity and transitivity of any inheritancerelation, as well as consistent use of field names across all objects of the same type (see Listing 2). A full example-module owdiff\_DT3\_DT2\_module.als is included in the doc-folder of the GitHub-project.

```
// ensures inheritance remains anti-symmetric
  fact NoCyclicInheritance {
    all t1: Type | all t2: Type |
     {t2 in t1.super} && {t1 in t2.super} => {t1 = t2}
  }
  // reflexivity and transitivity of inheritance
  fact ReflexiveTransitiveInheritance {
    all t1: Type | t1 in t1.super
    all t1: Type | all t2: Type |
10
      {t2 in t1.super} => {t2.super in t1.super}
11
  }
12
13
14 // consistent use of field names for all objects
  // of the same type
15
  fact ConsistencyOfGet {
16
    all src: Obj | all q : FName |
17
18
      some src.get[q] => {
19
      {src.get[q] in EnumVal and
20
        {one e:Enum |
          ObjAttrib[src.type.inst,q,e.values]}} or
      {src.get[q] in Val and
22
        {one v:Val | ObjAttrib[src.type.inst,q,v]}} or
23
24
      {src.get[q] in Obj and
```

21

<sup>&</sup>lt;sup>1</sup> https://github.com/MontiCore/cd4analysis/tree/ develop/src/cddiff/java/de/monticore/cddiff/ cd2alloy/generator

{some target : Type | all o : src.type.inst | o.get[q] in target.inst}}} 27 }

Listing 2 Additional type-related facts for open-world semantic differencing.

25 26

## 7. Solution II: Open-to-Closed-World Reduction

Our second approach for open-world semantic differencing reduces the analysis to closed-world semantic differencing via a transformation of the input-CDs. The transformation relies on the existence of a common abstract super-class *Object*. We specify the transformation as follows:

**Transformation** Let  $traf : CD \times CD \rightarrow CD \times CD$  such that for traf(A, B):

- 1. Every class exclusive to B is added to A as a non-abstract class without extends-relations.
- 2. We set  $c \prec_A Object$  for every class c in A without extendsrelation.
- 3. We add a new non-abstract subclass  $c_{sub}$  to every abstract class c in A.
- 4. For each association  $(c_1, r_1, r_2, c_2)$  in B, we add an association  $(c_1, r_1, r_2, Object)$  with underspecified cardinalities to A, unless this conflicts with existing associations.
- 5. Every class exclusive to A is added to B as a non-abstract class without extends relations.
- 6. For each class in B and each of its super-classes in A we add an extends-relation, unless this causes inheritance cycles. Afterwards we remove redundant extends-relations.
- 7. We add each associations from A to B but leave cardinalities underspecified, unless this conflicts with existing associations.

The purpose of this transformation is to (1) prevent the existence of closed-world witnesses that are not also open-world witnesses by copying elements from A to B without causing syntactical errors and (2) add elements to A that induce a closed-world witness iff a semantic difference exists under an open-world assumption. The latter is achieved by, e.g., adding the exclusive classes from B to A without extends relation in order to induce type-differences as well as introducing super-associations of associations exclusive to B to A that target the common abstract super-class. Moreover, the addition of a non-abstract subclass to each abstract class in A allows their indirect instantiation without additional constraints.

Consider the CDs A and B depicted in Figure 6 as a concrete example: The transformation adds the class Task from B to A to allow its instantiation via the closed-world operator. The common abstract super-class Object and its non-abstract subclass ObjSub are added, as well. Moreover, an association from Employee to Object with role name todo is also added to A. This association allows the closed-world operator to create corresponding links between objects of type Employee and objects of any other type. To prevent incorrect witnesses, the elements of the resulting CD A' that are missing in CD B are copied. This includes the classes Object, ObjSub and Manager, as well as corresponding associations and extends-relation. The OD *todoDiff* presents a potential diff-witness found by the closed-world operator after transforming the input CDs. Note that the Task accounting is not a todo for any Employee. Instead, we find that the Employee bob has a todo that is not a Task. Both of these circumstances are in violation of the semantic constraints implied by the association in the CD B. As such, we find that  $todoDiff \in [\![A]\!]^{ow} \setminus [\![B]\!]^{ow}$ .

We now demonstrate that this transformation in combination with a closed-world differencing operator is sufficient to detect open-world semantic differences in conflict-free finitelysatisfiable CDs.

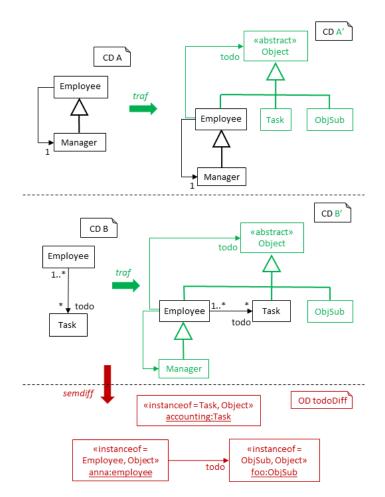


Figure 6 Example for reduction-based diff.

In the following let A and B be arbitrary conflict-free finitelysatisfiable CDs and let (A', B') := traf(A, B). We first show that finite satisfiability of the first input-CD A is preserved by the transformation.

## **Lemma 7.1.** A' is conflict-free and finitely-satisfiable.

*Proof.* By construction A' is conflict free. Since all associations in A' that are not present in A have no cardinality constraints, it follows that for every object structure  $os \in [\![A]\!]^{cw}$ , we find that  $os \in [A']^{cw}$  holds, as well. Thus, any class that is both in A

and A' is finitely-satisfiable in A'. Furthermore, any class in A' that is not present in A, extends at most 1 class. We conclude that these classes must also be finitely-satisfiable in A'.

Next we proof that the reduction is sound, *i.e.*, that any witness produced by the closed-world semantic differencing operator for the transformed input-CDs is a witness for a semantic difference under the open-world assumption.

**Theorem 7.2** (Soundness). If  $os \in [\![A']\!]^{cw} \setminus [\![B']\!]^{cw}$  then  $os \in [\![A]\!]^{ow} \setminus [\![B]\!]^{ow}$ .

*Proof.* Since A' is by construction an expansion of A, it follows that for every  $os \in [\![A']\!]^{cw}$ , we also have  $os \in [\![A]\!]^{ow}$ . Next, we proof by contradiction that for any  $os \in [\![B]\!]^{ow} \cap [\![A']\!]^{cw}$ , we also have  $os \in [\![B']\!]^{cw}$ . Assume this is not the case. Then there exists an object structure  $os \in [\![B]\!]^{ow} \cap [\![A']\!]^{cw}$  such that  $os \notin [\![B']\!]^{cw}$ . First, we conclude that there exists an expansion  $B^x$  of B such that  $os \in [\![B^x]\!]^{cw} \cap [\![A']\!]^{cw}$ . Second, it follows that os violates at least one condition outlined in Def. 4.3 with regards to B'. We now show that this cannot be the case:

- 1. A' and B' contain the same classes.
- 2. Since  $os \in [\![B^x]\!]^{cw} \cap [\![A']\!]^{cw}$ , for all  $o \in os.obj$  and all  $c \in A'.classes$ , it holds that  $o.type \prec^*_{A'} c$   $\iff c \in o.types$   $\iff o.type \prec^*_{B^x} c$ . Moreover, since  $\prec^*_{B^x}$  induces no inheritance-cycle, it then

follows from the transformation traf that  $o.type \prec^*_{A'} c \iff o.type \prec^*_{B'} c.$ 

- 3. For every  $(o_1, r_2, o_2) \in os.links$  there exists an association  $a = (c_1, r_1, r_2, c_2) \in A'.assoc$  with  $c_1 \in o_1.types$  and  $c_2 \in o_2.types$  that does not conflict with any association in *B*. Consequently, *B'* then also contains this association.
- 4./5. Every association in B' that is not also present in B has no cardinality constraints and is present in A', instead.
  - 6. Every bidirectional association in B' is also a bidirectional association in B.

Now all that is left is to demonstrate completeness of the reduction, *i.e.*, under the assumption that the closed-world semantic differencing operator finds a diff-witness if and only if a semantic difference in the closed world, the transformation ensures that an open-world diff-witness is found if a semantic difference exists in the open world.

By  $\hat{cd}$  we denote a minimal extension of CD cd to include super-class *Object* (if not already included).

**Theorem 7.3** (Completeness). If  $[\![A']\!]^{cw} \setminus [\![B']\!]^{cw} = \emptyset$  then  $[\![\hat{A}]\!]^{ow} \setminus [\![\hat{B}]\!]^{ow} = \emptyset$ .

*Proof.* This follows from Lemmas 7.4 and 7.5.  $\Box$ 

**Lemma 7.4.** If  $[\![A']\!]^{cw} \subseteq [\![B']\!]^{cw}$ , then  $[\![A']\!]^{ow} \subseteq [\![B']\!]^{ow}$ .

*Proof.* Assume that  $[\![A']\!]^{cw} \setminus [\![B']\!]^{cw} = \emptyset$ . Since A' and B' share the same classes and A' is finitely-satisfiable, B' must also be finitely-satisfiable. It follows that  $B'.abstract \subseteq$ 

A'.abstract. This also means that  $c_1 \prec_{A'} c_2 \iff c_1 \prec_{B'} c_2$ , i.e. both CDs must have exactly the same inheritance hierarchy. Furthermore, every association in A' must also be in B'. The same must hold for bidirectional associations, as well. Otherwise there would be an association in A' that is in conflict with an association in B'. Since A' is conflict-free, we would then be able to find an  $os \in [\![A']\!]^{cw} \setminus [\![B']\!]^{cw}$ . This, however, contradicts our assumption. By the same argument, it must follow that any non-redundant  $b \in \hat{B}.assoc$  is also in  $\hat{A}.assoc$ . Additionally, for every  $b = (c_1, r_1, r_2, c_2) \in B'.assoc$ , there is a sub-set of associations

$$S = \{(c'_1, r'_1, r_2, c'_2) \in A'.assoc : c_1 \prec^*_{B'} c'_1\}$$

such that  $\bigcap_{a \in S} A'.cardL(a) \subseteq B'.cardL(b)$  as well as  $\bigcap_{a \in S} A'.cardR(a) \subseteq B'.cardR(b)$ .

Since any abstract class  $c \in A'$ .*abstract* has a unique subclass, we conclude that any addition done equally to both A'and B' will have no effect on the semantic difference, and thus for every expansion  $(A')^x$  of A' and every  $os \in (A')^x$ , we can find an expansion  $(B')^x$  of B' such that  $os \in (B')^x$ , as well.  $\Box$ 

**Lemma 7.5.** If  $[\![A']\!]^{ow} \setminus [\![B']\!]^{ow} = \emptyset$ , then  $[\![\hat{A}]\!]^{ow} \setminus [\![\hat{B}]\!]^{ow} = \emptyset$ 

*Proof.* Since B' is an expansion of  $\hat{B}$  and any expansion of B' is also an expansion of  $\hat{B}$ , it follows that for all  $os_b \in [\![B']\!]^{ow}$ , we have  $os_b \in [\![\hat{B}]\!]^{ow}$ , as well. Now consider a  $diff \in [\![\hat{A}]\!]^{ow} \setminus [\![\hat{B}]\!]^{ow}$ . Without loss of generality, let  $c_{sub} \notin o.types$  for all  $o \in diff.obj$ , then  $diff \in [\![A']\!]^{ow} \setminus [\![\hat{B}]\!]^{ow} \square$ 

Note that, however, in the implementation of the closedworld operator CDDiff (Maoz et al. 2011b) all object models are bounded by a finite and typically small scope, which consequently also bounds the completeness of the open-world operator in practise.

#### Extension: Variability Open-/Closed-World Differencing

We have extended our transformation with a variability mechanism allowing the combination of open- and closed-world semantics interpretation of elements in both input-CDs. The extension is configured via UML/P stereotypes. Individual classes can be marked as «complete», then no super-classes and outgoing associations can be added. Furthermore, the CD itself can be marked as «complete», as well. This prevents any additions to the set of classes, the set of associations and the extends relation. In this manner, we are able to select an input-CD or specific elements of the CD that should be considered under a closedworld assumption. This is useful when comparing a predecessor version of a CD to a *final version* that should not be expanded, or alternatively if specific class declarations should not be expanded from a predecessor to a successor version, because it might constitute a breaking change with respect to a current implementation or violate existing requirement specification.

For example, consider the CD v3 depicted in Figure 3: If we consider this CD as our *final version* and mark it as *«complete»*, then no additions to the extends relation can be made. As such, any instance of the abstract class System must also be and instance of Machine (note that the class OtherSystem is not part of the CD at this point). Consequently, we have refined the

CD v2 depicted in Figure 2. This would otherwise not be the case as explained in Sect. 3.

In order to preserve completeness of the differencing operator, we extended the transformation to add outgoing dummy associations to classes in A that were only marked as *«complete»* in B. This necessarily will induce a diff-witness.

# 8. Implementation and Evaluation

The implementation of our open-world semantic differencing approaches have been integrated into the CDDiff-tool which is part of the larger CD4Analysis-project developed at the Chair of Software Engineering at RWTH Aachen University. The project is publicly available at https://github.com/ MontiCore/cd4analysis. CDDiff can be used as Javalibrary via the public methods that are provided by the CDDiff class or as a CLI-Tool via the MCCD.jar.

## 8.1. Running CDDiff for Open-World semantics

Recall the CDs from our motivating example in Sect. 3. Our implementation of the semantic differencing operator operates on the textual CD notation of CD4Analysis (Schindler 2012) with cd-files as input. We provide the files DigitalTwin1.cd, DigitalTwin2.cd and DigitalTwin3.cd in the doc folder of the CD4Analysis project.

Executing the MCCD.jar with the the following CLIcommand, we can compute the semantic difference of DigitalTwin2.cd and DigitalTwin1.cd.

```
java -jar MCCD.jar -i DigitalTwin2.cd --semdiff \
  DigitalTwin1.cd --open-world
```

The option --open-world uses the reduction-based approach introduced in Sect. 7 by default. Users may also specify the approach by choosing reduction-based or alloy-based as an argument.

Next we want to check whether DigitalTwin3.cd is a refinement of DigitalTwin2.cd. In order to reduce the potential size of diff-witnesses and thereby the search-space of the diffoperation, we may use the option --diffsize. If this option is not used, the maximum size of Alloy-solutions is set to twice the number of classes (and interfaces) in the input-CDs. We may also output the diff-witness as an od-file by specifying an output-directory with -o. More configuration options are documented in the README file. A link for downloading the MCCD.jar is also provided there.

```
java -jar MCCD.jar -i DigitalTwin3.cd --semdiff \
  DigitalTwin2.cd --open-world reduction-based \
    --diffsize 5 -o target/DT
```

A witness produced by the reduction-based implementation when executing this command is given in Listing 3. In addition to the witness, the implementation also outputs the transformed CDs for inspection.

```
objectdiagram witness_0 {
```

```
<<instanceof="Object, SystemSub4Diff, System">>
    SystemSub4Diff0:SystemSub4Diff;
    <<instanceof="DigitalTwin, Object">>
    DigitalTwin0:DigitalTwin;
    <<instanceof="DigitalShadow, Object">>
9
10
    DigitalShadow0:DigitalShadow;
11
    <<instanceof="DataTrace, Object">>
12
13
    DataTrace0:DataTrace ;
14
15
    <<instanceof="DataModel, Model, Object">>
    DataModel0:DataModel ;
16
17
    link DigitalTwin0 -> (models) DataModel0;
18
19
    link DigitalTwin0 -> (original) SystemSub4Diff0;
    link DigitalTwin0 -> (shadows) DigitalShadow0;
20
21
    link DigitalShadow0 -> (traces) DataTrace0;
22
    link DataTrace0 (traces) <-> (of) SystemSub4Diff0;
```

**Listing 3** A reduction-based diff-witness in the open-world semantics of DigitalTwin2.cd but not in the open-world semantics of the DigitalTwin3.cd

23

6

10

11

12

13

14

15

17

A witness produces by the Alloy-based implementation when executing the same command with the argument alloy-based instead of reduction-based is shown in Listing 4.

```
objectdiagram witness_0 {
  <<instanceof="DigitalShadow, DataTrace, Dummy4Diff
    , SystemSub4Diff, System">>
  SystemSub4Diff0:SystemSub4Diff;
  <<instanceof="ProcessModel, ModelSub4Diff,
    DigitalTwin, Dummy4Diff, Model">>
  ModelSub4Diff0:ModelSub4Diff;
  link SystemSub4Diff0 -> (original) SystemSub4Diff0;
  link SystemSub4Diff0 -> (original) ModelSub4Diff0;
  link SystemSub4Diff0 -> (of) SystemSub4Diff0;
  link SystemSub4Diff0 -> (traces) SystemSub4Diff0;
  link ModelSub4Diff0 -> (models) ModelSub4Diff0;
  link ModelSub4Diff0 -> (original) SystemSub4Diff0;
  link ModelSub4Diff0 -> (of) SystemSub4Diff0;
  link ModelSub4Diff0 -> (of) ModelSub4Diff0;
  link ModelSub4Diff0 -> (shadows) SystemSub4Diff0;
}
```

**Listing 4** An alloy-based diff-witness in the open-world semantics of DigitalTwin2.cd but not in the open-world semantics of the DigitalTwin3.cd

Unlike the witness from Listing 3, the one produced by the alloy-based implementation and shown in Listing 4 contains only two objects. These two objects instantiate multiple classes that were originally not related by inheritance in the input-CDs. This is a consequence of the Alloy Analyzer choosing to expand the extends-relation. Similarly, the role names of associations in the input-CDs have been reused for additional associations that are instantiated by links in the diff-witness, *e.g.*, the role name original is used to target the object ModelSub4Diff despite it not being an instance of type System. These additions may be considered to hinder browsing the diff-witness for relevant information on the semantic difference between the two input-CDs. In comparison, the diff-witness in Listing 3, which was

produced by the reduction-based implementation, contains no superfluous instances. We assume that, in general, the likelihood of superfluous instances is reduced for the reduction-based approach as the transformation employed by the reduction is deterministic and the closed-world operation that follows is not permitted to re-use role names or expand the extends-relation.

Before we conclude this sub-section, let us demonstrate a potential use of the stereotype *«complete»*. If we add *«complete»* at the start of line 3 in DigitalTwin3.cd and repeat the analysis, then no diff-witness is found. This is because now no additions to the extends-relation are permitted in the first input-CD and thus any instance of type System must also be an instance of type Machine.

#### 8.2. Evaluation

We are interested in two research questions:

- RQ1: How does the size and readability of computed witnesses differ between the encoding and the translation approach?
- RQ2: How does the performance differ between the encoding and the translation approach?

First, our translations employ different approaches to adding classes and relations between classes for computing open-world semantics. These might have an impact on the size and readability of computed diff witnesses.

Second, we believe that a performance evaluation is worthwhile as our two implementations of an open-world CDDiff operator are quite different in the techniques employed. We compare the performance of the operators in terms of ratios of their running times. Note that a comparison to the closed-world CDDiff from (Maoz et al. 2011b) would not be very meaningful, as open-world and closed-world semantic differencing are quite different problems.

Finally, we present our validation of both implementations in Sect. 8.3 and discuss threats to validity in Sect. 8.4.

We performed all experiments on an 11th Gen Intel Core i7-1185G7 CPU, 3.0 GHz, with 32 GB RAM, running Windows 10. Our implementation of the CDDiff operator uses the latest stable release of Alloy 6.0 with SAT4J as a SAT solver in its default configuration.

**8.2.1.** Corpus of CDs To evaluate our work, we have collected 25 pairs of consecutive versions of CDs (38 individual CDs) from different sources<sup>2</sup>. These sources are:

- 7 pairs of (11 individual) CDs from (Maoz et al. 2011b),
- 5 pairs of (10 individual) CDs manually created as part of this work to validate and evaluate general performance and edge cases, and
- 5 pairs of (10 individual) CDs of the CD4Analysis project<sup>3</sup>

Minor, syntactic modification had to be made to the latter two sets of CDs due to recent changes in the cd4analysis project.

**8.2.2. RQ1: Size and Readability** It is not straight forward how to evaluate the size and readability of generated diffwitnesses. A user-study is not in the scope of this work and we, instead, propose objective measures that may be taken as proxies for the readability of diff-witnesses. First, we consider the diff-witnesses with many objects and many links to be more difficult to read than those with fewer. Second, we consider CDs with object with low numbers of types per object to be easier to read than those with many types, i.e., more instances of objects in complex inheritance hierarchies.

Note that the numbers of objects and types per diff-witness are constrained by the diff-size parameter as an upper bound, which is not the case for the number of links. The latter is only constrained by the elements of the CDs. For our experiments we use diff-size = 5 as a reasonable default parameter of CDDiff. Also note that the diff-witnesses produced by our implementation are not necessarily unique, as the implementation relies on Alloy, which gives no guarantees in this regard.

For the translation-based open-world semantics, computed diff-witnesses across all CDs of our corpus have an average of 1.750 objects, 4.517 links, and objects are of 2.754 types on average. For the Alloy-based open-world semantics, computed diff-witnesses have an average of 2.133 objects, 2.033 links, and objects are of 2.195 types on average. The direct comparison between the two approaches shows that the Alloy-based approach produces diff-witnesses with less objects and more links, as well as more types per object. We presume that this is (1) because the Alloy Analyzer can arbitrarily expand the extends-relation and (2) because role names can be reused for new associations. The results are witnesses that are less readable.

**8.2.3. RQ2: Performance** We first tested the performance of both approaches using 5 pairs of synthetic CDs of increasing size. Each of these CDs was constructed to contain an equal number of classes and associations, as well as a proportional number of syntactic differences. Each diff operation was performed with two CDs of equal size ranging from 5 to 25 classes (in steps of 5). Table 1 (Alloy-based) and Table 2 (reduction-based) show the number of classes and associations of both input-CDs, as well as the corresponding running time in seconds for each open-world approach and various diff-sizes (ds, an upper limit on the size of diff-witnesses). Note that because of the Alloy Analyzer's non-determinism the reported running times may vary on different machines.

In order to better compare the two approaches regarding their performance we computed the running-time-ratios of Alloybased to reduction-based diff and displayed them in Table 3. Note that while the running times of the reduction-based approach start out slightly worse than for the Alloy-based approach, as the diff-size increases, the former overtakes the latter in terms of performance. Moreover, it appears that runningtimes-ratio of Alloy-based diff to reduction-based diff worsens as the input-CDs increase in size. This seems to indicate a greater running time complexity of the Alloy-based approach.

<sup>&</sup>lt;sup>2</sup> All CDs are available at: https://github.com/MontiCore/ cd4analysis/tree/develop/src/cddifftest/resources/ validation.

<sup>&</sup>lt;sup>3</sup> These are all CDs with at least two revisions from https://github .com/MontiCore/cd4analysis/tree/develop/doc at commit 5f48096.

CD size	ds=3	ds=5	ds=10	ds=15
5	0.847s	1.031s	1.969s	3.155s
10	0.516s	1.018s	3.068s	9.411s
15	1.120s	2.755s	12.091s	3.1360s
20	2.148s	5.833s	23.240s	72.002s
25	3.313s	8.210s	38.890s	142.491s

**Table 1** Running times of CDDiff for the Alloy-based openworld approach for increasing diff-sizes ds from 3 to 15 and increasing sizes of CDs from 5 to 25 classes

CD size	ds=3	ds=5	ds=10	ds=15
5	0.704s	0.837s	1.005s	2.084s
10	0.866s	1.203s	2.186s	3.530s
15	1.659s	3.037s	4.713s	11.599s
20	2.550s	3.314s	7.851s	17.140s
25	3.684s	4.759s	14.083s	27.199s

**Table 2** Running times of CDDiff for the reduction-basedopen-world approach for increasing diff-sizes ds from 3 to 15and increasing sizes of CDs from 5 to 25 classes

We continued testing the performance of both approaches using the CDs from (Maoz et al. 2011b). More, specifically we performed the diff operations by comparing the successor version of each diagram to its direct predecessor. We display the running-time-ratios in Table 4. Here, we found the same trends as before: increases in diff-size and size of the CD led to a better running-times-ratio for the reduction-based approach.

Finally, we evaluated the performance of both approaches on CDs from the CD4Analysis-project. We compared two versions of each CD. The running-time-ratios are displayed in Table 5 and confirm the trend observed before.

CD size	ds=3	ds=5	ds=10	ds=15
5	1.203	1.231	1.959	1.514
10	0.596	0.846	1.403	2.666
15	0.675	0.907	2.565	2.704
20	0.842	1.760	2.960	4.201
25	0.899	1.723	2.761	5.239
mean	0.843	1.293	2.330	3.265

**Table 3** Ratio of running times between the Alloy-based and the reduction-based analyses reported in Table 1 and Table 2.

CD pair	ds=3	ds=5	ds=10	ds=15
DE	3.644	4.327	3.398	2.865
EA	0.636	0.821	1.149	1.633
EMT	0.524	0.457	1.132	0.981
Library v2/v1	1.428	2.477	3.383	3.123
Library v3/v2	1.301	1.764	1.440	1.311
Library v4/v3	1.148	2.539	3.736	4.363
Library v5/v4	2.047	1.78	1.475	1.676
mean	1.290	1.804	2.234	2.291

**Table 4** Ratios of running times for the alloy-based and the reduction-based CDDiff analysis on CDs from (Maoz et al. 2011b) and different diff-sizes ds ranging from 3 to 15.

CD pair	ds=3	ds=5	ds=10	ds=15
Management	1.708	1.627	2.114	2.402
MyCompany	0.972	1.281	1.565	1.425
MyExample	0.695	0.554	1.461	2.094
MyLife	1.611	1.621	1.824	2.411
Teaching	0.623	0.870	1.608	1.923
mean	1.121	1.191	1.714	2.051

**Table 5** Ratios of running times for the alloy-based and the reduction-based CDDiff analysis on the CD4Analysis CDs and different diff-sizes ds ranging from 3 to 15.

#### 8.3. Validation

To ensure correct implementation of the extensions presented in Sect. 6 and Sect. 7, we have validated our work on many CD pairs, including the ones listed as the corpus of our evaluation. In particular, we have performed the following automated checks for diff-sizes 3, 5 and 10:

- Each CD is semantically equivalent to itself, *i.e.*, no diffwitnesses are produced (automatically determined).
- Each CD is a refinement of the empty CD, *i.e.*, no diffwitnesses are produced (automatically determined).
- Both implementations of open-world semantic differencing always agree on the existence and absence of diff-witnesses (automatically determined).
- No diff-witnesses are produced when comparing a refining successor version of a CD to its predecessor (determined by manual inspection).
- Diff-witnesses are produced when comparing a nonrefining successor version of a CD to its predecessor (determined by manual inspection).
- All diff-witnesses produced are sound (automatically determined, see below).

To verify the soundness of the produced witnesses, we devel-

oped the OD2CDMatcher<sup>4</sup>, a tool which can determine whether an object-structure in the form of an OD is in the semantics of a CD. Note that this tool relies on an alternative implementation and is independent of the encoding of CD semantics in Alloy used by the CDDiff operators. OD2CDMatcher can operate under both the closed-world and open-world assumption. As such, we not only verified the soundness of the witnesses with respect to the open-world semantics of the original input-CDs for both approaches, but for the reduction-based approach, we also checked the closed-world semantics of the transformed input-CDs. In this manner, we were able to identify and correct several issues in our implementation.

#### 8.4. Threats To Validity

First, the UML CD standardization (Object Management Group 2017) only describes the semantics of CDs using natural language and gives no formal definition of semantics. Our approach is built upon previous definitions of CD semantics, but other modelers might have a different interpretation. Similarly, other modelers may disagree with us permitting overlapping associations in CDs or our handling of underspecified associations. Overlapping associations are easily handled by a model analyzer such as Alloy, as they simply constitute a conjunction of logical constraints. They allow refinement of associations for sub-classes consistent with set logic and permitting them simplifies our implementation. Another assumption is the implicit existence of the super-type *Object*, on which the validity of our reduction-based approach depends. To mitigate the threat of ambiguity in semantics of CDs, we base our work on previously published implementations (Maoz et al. 2011b; Kautz et al. 2017) and make all new implementations publicly available.

Second, regarding our evaluation, we cannot guarantee that the legibility of diff-witnesses and running time of operations for larger CDs and greater diff-size will always be improved for the reduction-based approach compared to the Alloy-based approach. This was simply the case for the examples in this paper and further evaluation might be necessary to make generalized claims. To mitigate the threat of a biased selection we have included previously published CDs in our evaluation that were not created specifically for open-world semantic differencing.

Third, our experiments use a single SAT solver in the default configuration as provided by Alloy. It is well-known that different SAT solver may lead to different performance results (Wang et al. 2019). To mitigate this threat of varying performance results, we have selected SAT4J for all experiments as the default and reportedly most stable SAT solver bundled with Alloy.

Finally, the answer to RQ1 relies on the diff-witnesses produced by Alloy. These diff-witnesses are not unique and may be different on different machines and software configurations. To mitigate the threat of different possible solutions, we have calculated averages over multiple pairs of CDs, we have captured the diff-witnesses produced on our machine, and we make all data available for inspection and comparison.

## 9. Conclusion and Outlook

In this paper, we outlined two approaches for open-world semantic differencing for UML/P CDs to assist change management in the early design phases of MDD. Both approaches extend the operator CDDiff introduced in (Maoz et al. 2011b). Furthermore, we demonstrated that the problem of open-world semantic differencing can be reduced to closed-world semantic differencing by comparing appropriate CD-expansions of the input-CDs, a fact that both approaches exploit: The first approach uses the Alloy Analyzer to implicitly construct and consider these expansions, while the second approach directly transforms the input-CDs based on a deterministic transformation algorithm. Our evaluation found that the transformation-based approach yields more readable diff-witnesses in shorter time.

We extended our approach to enable modelers to specify individual input-CDs or elements of a CD that should be considered under the closed-world assumption when computing an open-world difference: Marking a class with the stereotype *«complete»* forbids additional super-classes and additional outgoing associations. Marking the whole CD with the stereotype *«complete»* forbids additions to the set of classes, set of associations, and the inheritance relations of classes.

As future work, additional stereotypes could be introduced to allow for more semantic variability, *e.g.*, a class might be marked as *«sealed»* to forbid additional sub-classes. In the future, we also intend to conduct a case-study on the usefulness of automatic refinement checking and semantic differencing with CDDiff when designing object-oriented software.

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<sup>&</sup>lt;sup>4</sup> The tool is included in the CD4Analysis-repository on GitHub at: https://github.com/MontiCore/cd4analysis

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